



Conflicts in Abstract Argumentation¹

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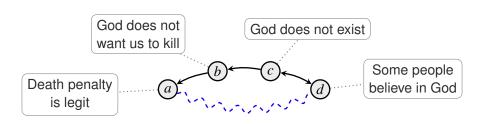
DBAI research seminar, November 10, 2016



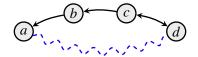


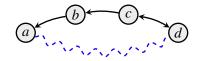
¹This research has been supported by FWF (projects I1102 and I2854).

Argumentation



Natural Language Example, Is Death Penalty Legit?





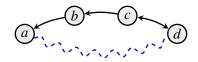
- Arguments: a, b, c, d
- Attacks: (b, a), (c, b), (d, c), (c, d)

Definition (Abstract Argumentation, Syntax)

Argumentation Framework (AF): F = (A, R)

A: set of arguments

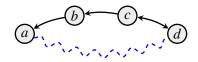
 $R \subseteq A \times A$: set of attacks



- Arguments: a, b, c, d
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- ullet Conflicts: [a,b],[b,c],[c,d]

Definition (Syntactic Conflict and Compatibility)

Syntactic Conflict, $[X,Y]_F$: X attacks Y or Y attacks X Syntactic Compatibility, $\{X,Y\}_F$: otherwise

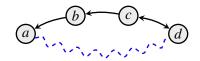


- Arguments: a, b, c, d
- Attacks: (b, a), (c, b), (d, c), (c, d)
- Extensions: $\{a, c\}, \{b, d\}$

Definition (Argumentation Semantics)

Conflict-freeness, $S \in \mathit{cf}(F)$: $\{S, S\}_F$

Stable Extension, $S \in sb(F) \subseteq cf(F)$: $A \setminus S = \{x \in A \mid S \text{ attacks } x\}$

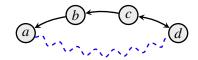


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Definition (Semantic Conflict and Compatibility)

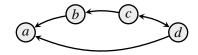
Semantic Compatibility, $\{X,Y\}_{\mathbb{S}}$: f.a. $x\in X,y\in Y$ ex. $S\in \mathbb{S}$, $\{x,y\}\subseteq S$ Semantic Conflict, $[X,Y]_{\mathbb{S}}$: otherwise

Framework Modifications



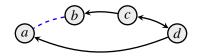
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Framework Modifications

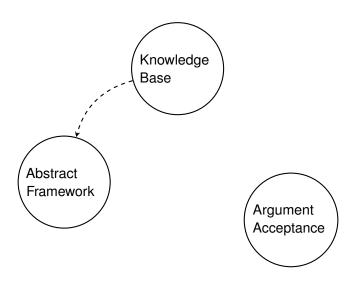


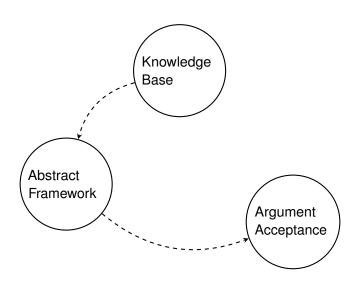
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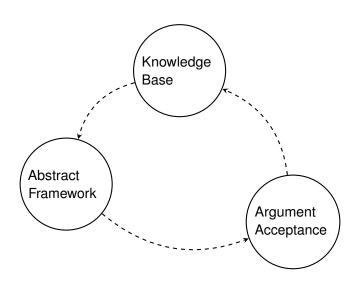
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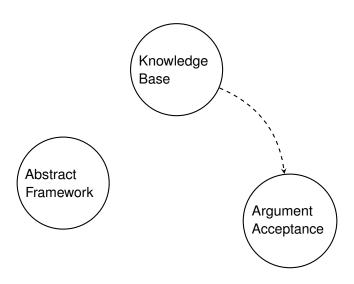


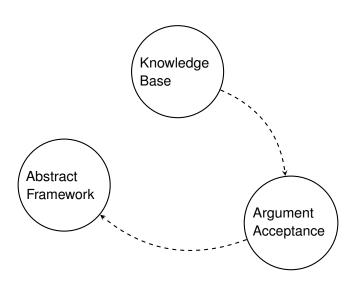
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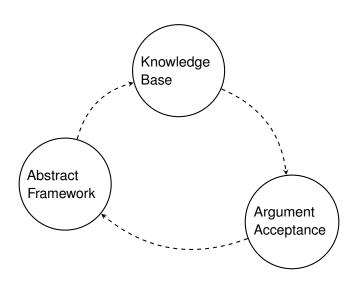












Realizability and Conflict

Definition (Realizability)

- $\mathbb S$ is σ -realizable if ex. AF F with $\sigma(F)=\mathbb S$
- $\mathbb S$ is σ_A -realizable if ex AF F=(A,R) with $\sigma(F)=\mathbb S$

Definition (Conflict)

A semantic conflict $[a,b]_{\mathbb{S}}$ is

- *pure* (semantic) if there is no realization F with $[a,b]_F$;
- necessary (syntactic) if any realization F has $[a,b]_F$;
- optional otherwise.

Levels of Conflict

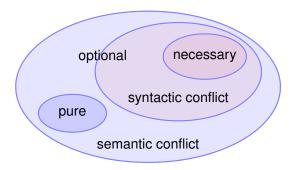
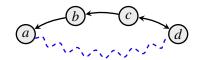


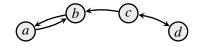
Figure: A Venn-diagram illustrating different levels of conflict.

Arbitrary Modifications



- Arguments: a, b, c, d
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Arbitrary Modifications



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Conflict Characterizations

Theorem (Stable Conflicts)

 $[a,b]_{\mathbb{S}}$ is necessary attack $(a,b)_F$ for each sb-realization F of \mathbb{S} if and only if there is $S \in \mathbb{S}$, $a \in S$ and $\{b,S \setminus \{a\}\}_{\mathbb{S}}$.

All other conflicts for sb are optional.

Modifications for Stable Semantics

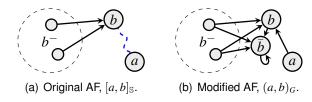


Figure: Forcing attacks for stable semantics.

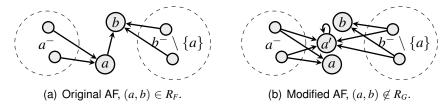


Figure: Purging Attacks for Stable Semantics.

Illustration of Stable Modifications

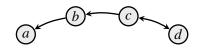
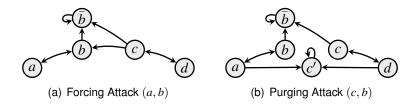


Figure : Original AF.



Realizability and Conflict

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Definition (Conflict)

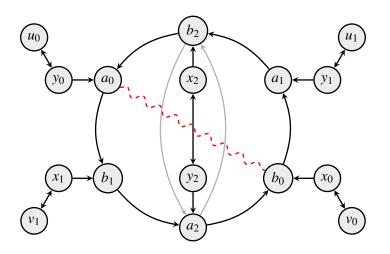
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Definition (Conditional Conflicts)

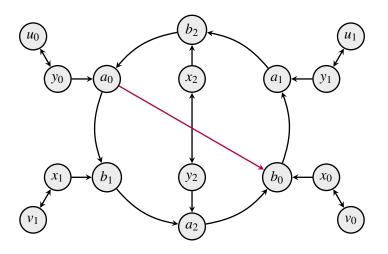
Extend pure, necessary and optional to A-realizability

A-Purity



Argument set of interest: $\{a_0, a_1, y_2, u_0, u_1, v_0, v_1\}$

A-Purity



Argument set of interest: $\{a_0, a_1, y_2, u_0, u_1, v_0, v_1\}$

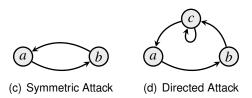
Conclusions

For Stable Semantics

- necessary Conflicts can be directed (attacks) or undirected (symmetric attacks);
- in general there are no pure conflicts;
- A-purity however is possible;
- one could allow bigger extensions to get rid of necessary conflicts;
- manipulation only requires compatibilities.

Other Semantics

- Preferred and Semi-stable semantics have only symmetric necessary attacks [a,b] where there are $S,T\in\mathbb{S}$ with $a\in S,b\in T$ and otherwise compatibilities $\{a,T\setminus\{b\}\}_{\mathbb{S}},\{b,S\setminus\{a\}\}_{\mathbb{S}}.$
- Stage semantics has the same necessary conflicts as Stable, but without directions.
- Cf2 semantics probably has the same necessary conflicts as Stable, no necessary symmetric attacks but allows general pure conflicts.



Future Work, Open Questions

- Conflicts between sets of arguments.
- Conditional Conflicts: exact characterizations for *A*-pure definitions, under what circumstances can *A*-pure conflicts arise?
- Formal definition of attack-minimal AFs
- Other semantics, labellings, ...
- Instantiation-related questions; what does it mean to use such modifications? How can we use this knowledge to manipulate or analyse/detect manipulation?
- Other directions: Given some AF, which arguments necessarily are jointly acceptable? How can we detect semantic conflicts without computing all extensions?
- Syntactic Conflict is a semantics, extend approach to arbitrary pairs of semantics.

References

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- Dung, P. M. (1995).
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Preferred Modifications

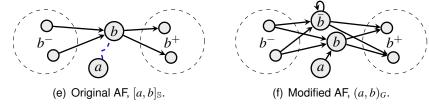


Figure: Forcing Attacks for Preferred Semantics.

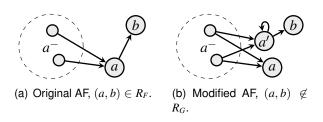


Figure: Purging Attacks for Preferred Semantics.

Illustration of Preferred Modifications.

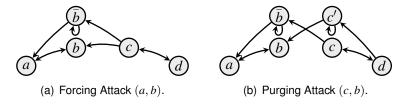


Figure : Analogy to Stable Illustration.

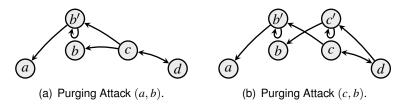


Figure: For an attack-minimal AF.