

# Computational Models of Argumentation: A Fresh View on Old AI Problems

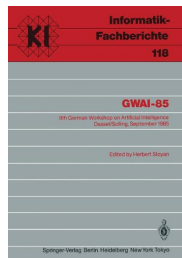
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joint work with S. Ellmauthaler, H. Strass, J. Wallner, S. Woltran



My very first conference: 9th KI 1985  
(formerly known as GWAI)



KR session:

- John McCarthy: *What is Common Sense and How to Formalize it?*
- Gerhard Brewka: *Über normale Vögel, anwendbare Regeln und einen Default-Beweiser.*
- Peter Schefe: *Zur Rekonstruktion von Wissen in neueren Repräsentationssprachen der Künstlichen Intelligenz.*
- Kai von Luck, Bernhard Nebel, Christof Peltason, Albrecht Schmiedel: *BACK to Consistency and Incompleteness.*

# Good Times for AI - Bad Times for Logicians?



- Due to some major breakthroughs AI in the media more than ever
- IJCAI-17 close to 2100 attendees, 2500 submissions; AAAI-18 3800(!) submissions
- Germany's digital association Bitkom demands 4 billion Euros + 40 additional professorships for AI research in Germany
- Much of this attributed to successes in deep learning
- True, but ... a closer look often reveals intricate combination of learning and "classical" AI methods

# A Prominent Example: Google Deep Mind's AlphaGo



- widely perceived as neural network; but (Darwiche/Etzioni):
- *"AlphaGo is not a neural network since its architecture is based on a collection of AI techniques ... in the works for at least fifty years."*
- minimax technique for two-player games, stochastic search, learning from self play, evaluation functions to cut off minimax search trees, reinforcement learning, in addition to neural nets.

- Sandholm's Libratus, beating a team of four top pros in poker, powered by new, domain-independent algorithms for
  - computing approximate Nash equilibrium strategies beforehand,
  - endgame solving during play, and
  - fixing its own strategy to play even closer to equilibrium based on what holes the opponents have been able to identify and exploit.
- Dan Roth (IJCAI 2017 John McCarthy Award): success in NLP will be limited unless reasoning gets involved
- Wahlster, KI 2017: "Without good planning techniques the vision of Industrie 4.0 will not come true"
- "There is life in AI outside deep learning" R. Lopez de Mantaras

# The Case of Explainability

- To gain user confidence, AI systems must be able to explain their recommendations and actions
- Black box often unsuitable; not understanding brain no excuse
- Explanation: *a reason or justification given for an action or belief* (online dictionary)
- *Reasoning* the main object of study of a logician, so why worry?
- But: AI logicians need to be open to deviate from classical techniques



Explanation Master Course

Develop powerful explanation skills for any situation or medium.

## Be prepared to work

- with inference based on some specific (preferred) rather than all models
- with inference relations that are nonmonotonic as what is preferred may change with new information
- with partial rather than complete interpretations as sometimes there is no reasonable way to assign a truth value
- with modern, operator-based techniques to single out the preferred semantic objects, e.g. as fixpoints of these operators
- with multiple semantics, as different situations may require different inferences
- with representations users want, which may look very different from classical logic syntax, e.g. labelled graphs

# How Does Argumentation Come In?

Modgil/Prakken AIJ 2013:



Form of reasoning that *makes explicit the reasons for the conclusions drawn and how conflicts between reasons are resolved.*

Provides *natural mechanism to handle inconsistent and uncertain information* and to resolve conflicts of opinion.

Argumentation approach bridges gap [between logic and human reasoning] by providing *logical formalisms rigid enough to be formally studied ...*, while being *close enough to informal reasoning ...*

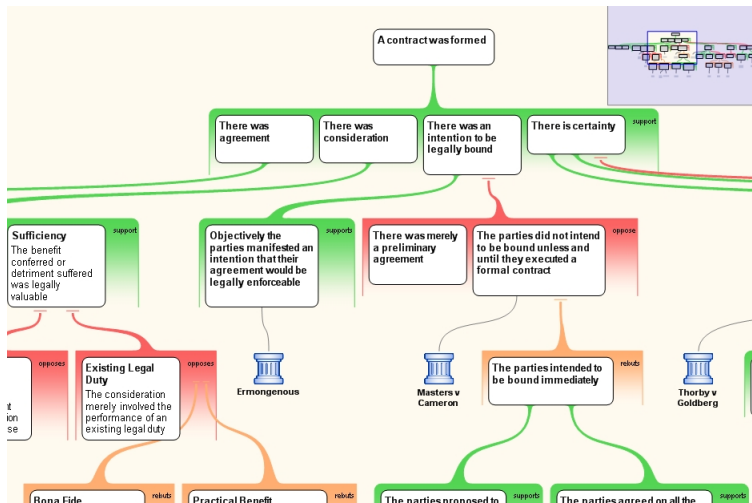


# Graphs as Knowledge Representation Languages



- Graphical representations extremely popular: semantic nets, rdf graphs, knowledge graphs, argument graphs
- Easy to construct, easy to read by humans, easy to maintain
- Links often represent 2-place predicates, nodes their arguments
- Focus here on **acceptance graphs**:  
nodes represent statements, positions, arguments ...,  
links relationships between the former, e.g. support, attack ...
- Main goal: identify nodes that can reasonably be accepted

# Motivation: Argument Mapping



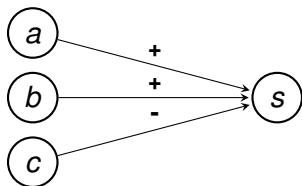
T. Gordon: "*It's graphs what you want to present to the audience ...*"

- Labelled graphs conveniently visualize argumentation scenarios
- Nodes propositions, statements, arguments ... whatever can be accepted or not
- Links represent relationships, labels the type of the relationship
- But what do the links really mean?
- Want to use maps not only for visualization, but for *evaluation*
- Requires a framework for specifying semantics!

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# Another Example



Should  $s$  be accepted? Various options, e.g.

- no negative and all positive links are active, or
- no negative and at least one positive link is active, or
- more positive than negative links are active.

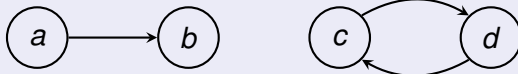
Bottom line: need an acceptance condition for each of the nodes.

- 1 Setting the Stage (done)
- 2 A Precedent: Dung's Argumentation Frameworks
- 3 A Step Forward: Abstract Dialectical Frameworks
- 4 From ADFs to GRaph-based Argument Processing (GRAPPA)
- 5 Conclusions

## 2. A Precedent: Dung Frameworks

### Abstract Argumentation Frameworks (AFs)

- immensely popular in the argumentation community
- syntactically: directed graphs



- conceptually: nodes arguments, edges attacks between arguments
- semantically: *extensions* are sets of “acceptable” arguments
- a simple special case of labelled graphs:  
single label (left implicit), fixed acceptance condition

$F = (A, R)$  an argumentation framework,  $S \subseteq A$ .

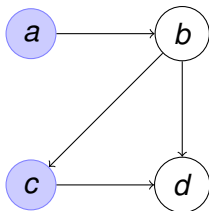
- $S$  *conflict-free*: no element of  $S$  attacks an element in  $S$ .
- $a \in A$  *defended* by  $S$ : all attackers of  $a$  attacked by element of  $S$ .
- a conflict-free set  $S$  is
  - *admissible* iff it defends all arguments it contains,
  - *preferred* iff it is  $\subseteq$ -maximal admissible,
  - *complete* iff it contains exactly the arguments it defends,
  - *grounded* iff it is  $\subseteq$ -minimal complete,
  - *stable* iff it attacks all arguments not in  $S$ .

## Main goal:

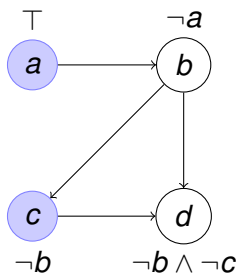
Generalize what Dung did for simple AFs to arbitrary labelled graphs.



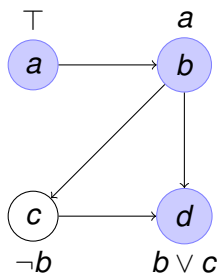
### 3. ADFs: Basic Idea



An Argumentation Framework



An Argumentation Framework  
with explicit acceptance conditions



A Dialectical Framework  
with flexible acceptance conditions

# Background on ADFs

- Directed graph, each node has explicit acceptance condition expressed as propositional formula.
- ADFs properly generalize AFs under major semantics.
- Semantics based on operator  $\Gamma_D$  over partial (3-valued) interpretations (here represented as consistent sets of literals).
- Takes interpretation  $v$  and produces a new (revised) one  $v'$ .
- $v' = \Gamma_D(v)$  makes a node  $s$ 
  - **t** iff acceptance condition true under all 2-valued completions of  $v$ ,
  - **f** iff acceptance condition false under all 2-valued completions of  $v$ ,
  - undefined otherwise.
- Operator thus checks what can be justified based on  $v$ .

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## An interpretation $v$ of ADF $D$ is

- a *model* of  $D$  iff  $v$  is total and  $\Gamma_D(v) = v$ .  
Intuition: statement is **t** iff its acceptance condition says so.
- *grounded* for  $D$  iff it is the least fixpoint of  $\Gamma_D$ .  
Intuition: collects information beyond doubt.
- *admissible* for  $D$  iff  $v \subseteq \Gamma_D(v)$   
Intuition: does not contain unjustifiable information
- *preferred* for  $D$  iff it is  $\subseteq$ -maximal admissible for  $D$   
Intuition: want maximal information content.
- *complete* for  $D$  iff  $v = \Gamma_D(v)$ .  
Intuition: contains exactly the justifiable information.

Stable semantics: reduct-based check as in logic programming.

# Stable Models for ADFs

Based on ideas from Logic Programming:

- no self-justifying cycles,
- achieved by reduct-based check.

To check whether a two-valued model  $v$  of  $D$  is *stable* do the following:

- eliminate in  $D$  all nodes with value **f** and corresponding links,
- replace eliminated nodes in acceptance conditions by **f**,
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- ADFs properly generalize AFs.
- All major semantics available.
- Many results carry over, eg. the following inclusions hold:

$$sta(D) \subseteq val_2(D) \subseteq pref(D) \subseteq com(D) \subseteq adm(D).$$

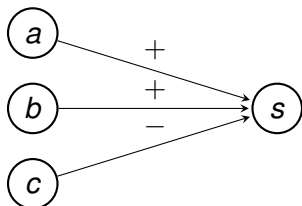
- for ADFs corresponding to AFs models and stable models coincide (as AFs cannot express support).
- various results regarding realizability, complexity, ...
  - ADFs CANNOT in general be translated to AFs in polynomial time.
  - Same complexity in case of **bipolar** ADFs.
  - Shows that in this case additional expressiveness comes for free.

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# Using ADFs: Earlier Example



- Positive and negative links
- Acceptance condition of *s*:
  - no negative and all positive links active:  $\neg c \wedge (a \wedge b)$
  - no negative and at least one positive link active:  $\neg c \wedge (a \vee b)$
  - more positive than negative links active:  $(\neg c \wedge (a \vee b)) \vee (a \wedge b)$
- Acceptance condition defined individually for each node

## 4. From ADFs to GRAPPA

- Compiling argumentation graphs to ADFs tedious in general
- Can we define ADF-like semantics directly for any labelled graph?
- YES, requires
  - to define acceptance conditions in terms of labels of active links
  - and adequate modification of characteristic operator
- The rest basically falls into place
- Main advantages:
  - Closer to graphical models people use
  - Same intuition has same representation for all nodes, e.g.  
 $\#+ > \#-$  rather than node specific prop. formula

# From ADFs to GRAPPA, ctd.

- Acceptance conditions based on **multisets of labels of active links**
- **New characteristic operator** taking these into account

An acceptance function over labels  $L$  is a function  $c : (L \rightarrow \mathbb{N}) \rightarrow \{t, f\}$ .

A labelled argument graph (LAG) is a tuple  $G = (S, E, L, \lambda, \alpha)$  where

- $S$  is a set of nodes (statements),
- $E$  is a set of edges (dependencies),
- $L$  is a set of labels,
- $\lambda : E \rightarrow L$  assigns labels to edges,
- $\alpha : S \rightarrow F^L$  assigns  $L$ -acceptance-functions to nodes.

# The Characteristic Operator $\Gamma_G$

- Operator revises partial interpretation  $v$ , produces new one  $v'$ .
- Checks which truth values of nodes in  $S$  can be justified by  $v$ .
- Done by considering all possible completions of  $v$  and their induced multisets of active labels:
  - if acceptance function of  $s$  yields  $t$  under all such multisets, then  $v'$  assigns **t** to  $s$ .
  - if acceptance function of  $s$  yields  $f$  under all such multisets, then  $v'$  assigns **f** to  $s$ .
  - otherwise the value remains open.
- Basically the same as for ADFs, except for acceptance functions involved.

As for ADFs

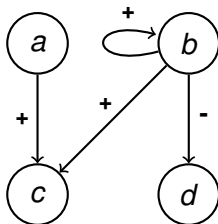
Let  $G = (S, E, L, \lambda, \alpha)$  be an LAG,  $v$  a partial interpretation of  $S$ .

- $v$  is a model of  $G$  iff  $v$  is total and  $v = \Gamma_G(v)$ ,
- $v$  is grounded in  $G$  iff  $v$  is the least fixed point of  $\Gamma_G$ ,
- $v$  is admissible in  $G$  iff  $v \subseteq \Gamma_G(v)$ ,
- $v$  is preferred in  $G$  iff  $v$  is  $\subseteq$ -maximal admissible in  $G$ ,
- $v$  is complete in  $G$  iff  $v = \Gamma_G(v)$ .

Stable models: no self-justifying cycles. Checked by LP-style reduct.



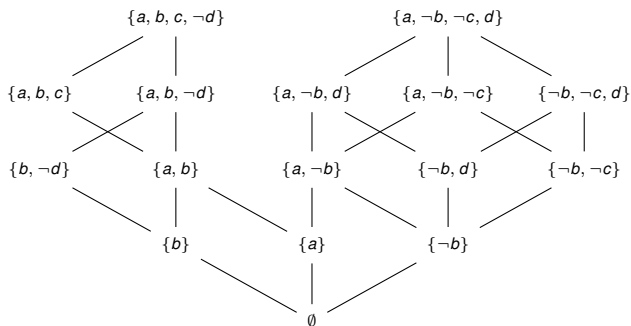
# Example



Acceptance condition for all nodes: all positive links active, no negative link active.

# Example, ctd.

16 admissible interpretations:



Models:  $\{a, b, c, \neg d\}$ ,  $\{a, \neg b, \neg c, d\}$ .

Grounded:  $\{a\}$ .

Preferred:  $\{a, b, c, \neg d\}$ ,  $\{a, \neg b, \neg c, d\}$ .

Complete:  $\{a, b, c, \neg d\}$ ,  $\{a, \neg b, \neg c, d\}$ ,  $\{a\}$ .

# The GRAPPA Pattern Language

- How to express acceptance conditions?
- Developed pattern language for this purpose.
- Can refer to number of total and active labels of specific types; to minimal/maximal elements; simple arithmetics and relations.
- Won't define language completely, illustrate it with examples.
  - Let  $L = \{++, +, -, --\}$
  - Assume node accepted if support stronger than attack, measure strength by counting respective links; multiply strong support/attack with a factor of 2.
  - Describe this using pattern:

$$2(\#++) + (\#+) - 2(\#--) - (\#-) > 0.$$

## Dung AFs

Single label - left implicit. Single pattern for all nodes:

- no negative active link:  $(\#-) = 0$

## ADFs

ADF acceptance conditions propositional formulas. GRAPPA: label each link with its source node. Pattern:

- replace each occurrence of atom  $a$  in ADF acceptance condition by the basic pattern  $\#a = 1$ .

## Bipolar argument graphs

Labels for support (+) and attack (-). Possible acceptance conditions:

- all positive, no negative link active:  $(\#_{t+}) - (\#_{+}) = 0 \wedge (\#_{-}) = 0$ ,
- at least one positive, no negative active link:  $(\#_{+}) > 0 \wedge (\#_{-}) = 0$ ,
- more positive than negative active links:  $(\#_{+}) - (\#_{-}) > 0$ .

## Weighted argument graphs

Labels positive or negative numbers. Various possible patterns:

- the sum of weights of active links is greater than 0:  $sum > 0$ .
- the highest active support is stronger than the strongest (lowest) attack:  $max + min > 0$
- the difference among strongest active support and the strongest active attack is above some threshold  $b$ :  $max + min > b$ .

## Proof standards (Farley and Freeman)

Framework for expressing proof standards based on 4 types of arguments: valid, strong, credible and weak.

Need 8 labels  $v, s, c, w, -v, -s, -c, -w$ . Patterns of some of the proof standards:

- scintilla of evidence:  $\#\{v, s, c, w\} > 0$
- dialectical validity:  $\#\{v, s, c\} > 0, \#\{-v, -s, -c, -w\} = 0$
- beyond reasonable doubt:  $\#\{v, s\} > 0, \#\{-v, -s, -c, -w\} = 0$
- beyond doubt:  $\#v > 0, \#\{-v, -s, -c, -w\} = 0$

## **Carneades** (Gordon, Prakken, Walton)

Argument graphs with 2 types of nodes. Pattern for argument nodes:

- $(\#_{t+}) - (\#_{+}) = 0 \wedge (\#_{-}) = 0$ ,

Patterns for proposition nodes ( $\alpha, \beta$  and  $\gamma$  numerical parameters):

- scintilla of evidence:  $max > 0$
- preponderance of evidence:  $max + min > 0$
- clear and convincing evidence:  $max > \alpha \wedge max + min > \beta$
- beyond reasonable doubt:  $max > \alpha \wedge max + min > \beta \wedge -min < \gamma$
- dialectical validity:  $max > 0 \wedge min > 0$

## 5. Conclusions

- Presented a semantical framework for labelled argument graphs
  - based on ideas from ADFs, yet domain of acceptance conditions multisets of labels,
  - pattern language for expressing acceptance conditions,
  - demonstrated generality by reconstructing various systems,
  - implementations by compilation to ADFs.
- What does GRAPPA buy you?
  - pick your favourite graphical representation of argumentation scenarios
  - turn it into a well-founded formalism with full range of Dung semantics
  - by specifying patterns in a convenient language.



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- System development, based on DIAMOND, our ADF solver
- Mobile App *ArgueApply*, LPNMR-17 best system description
- Extension to weighted case: partial multi-valued interpretations
- Application to interesting argument graphs